

The Intersectionality Problem for Algorithmic Fairness

Johannes Himmelreich¹

Arbie Hsu²

Kristian Lum³

Ellen Veomett²

¹Syracuse University

²University of San Francisco

³University of Chicago



Problem: Statistical Uncertainty

Intersectionality makes typical fairness definitions meaningless because of statistical uncertainty due to increasingly small subgroups

- **Intersectionality:** Fairness for *subgroups*
 - e.g., for **Maghrebi older women in France** simultaneously
 - instead of each **ethnic origin, age, gender, location** separately
- **But:** Number of intersectional subgroups grows exponentially:
 - $\prod k^n$ (for n k -valued attributes)
- **Thus:** High **statistical uncertainty** in fairness “metrics”
- **Problem:** Widely-used definitions of **fairness** become meaningless

$$|m(G) - m(\cdot)| < \epsilon \quad \forall G$$

where $m(\cdot)$ $m(G)$ model performance (however understood) for group G

Solutions: Desiderata

Based on consensus in literature, uncontroversial assumptions

1. **Minimal Justice:** Don't lower fairness standard for certain groups; i.e., “don't disadvantage the disadvantaged”
2. **Incentive Compatibility:** Don't discourage further data collection, and don't encourage deliberate mistakes

Existing Solutions Violate Desiderata

Example: Kearns et al. (2018)

$$\alpha(G) |m(G) - m(\cdot)| < \epsilon \quad \forall G$$

where $\alpha(G) = \Pr(G)$, proportion of group G in population

- **Violates Minimal Justice:** fairness proportional to group size
 - small groups are often disadvantaged, i.e., *less* fairness for them
- **Violates Incentive Compatibility**
 - discourages minority group data collection (since model subgroup performance is typically lower than current estimate)
 - generally, one *can* improve fairness by making deliberately inaccurate predictions (on group with high model performance)

Alternative: Metrics Based on Hypothesis Testing

Optimist's Metric

Null hypothesis: Model is **fair**

$$H_0 : m(G) > c \quad \forall G$$

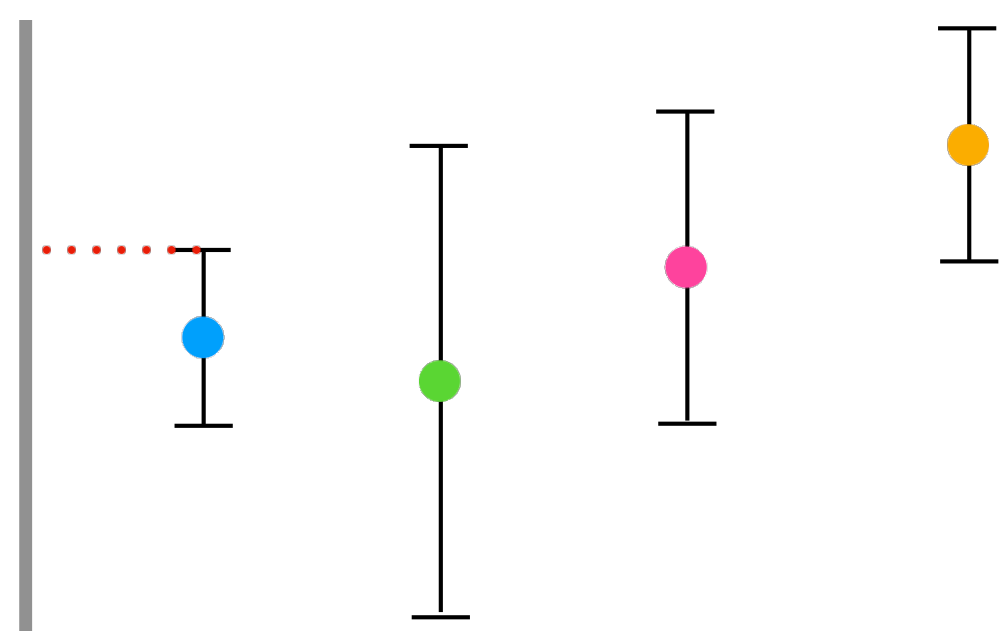
$$H_1 : m(G) \leq c \quad \exists G$$

Pessimist's Metric

Null hypothesis: Model is **unfair**

$$H_0 : m(G) < c \quad \exists G$$

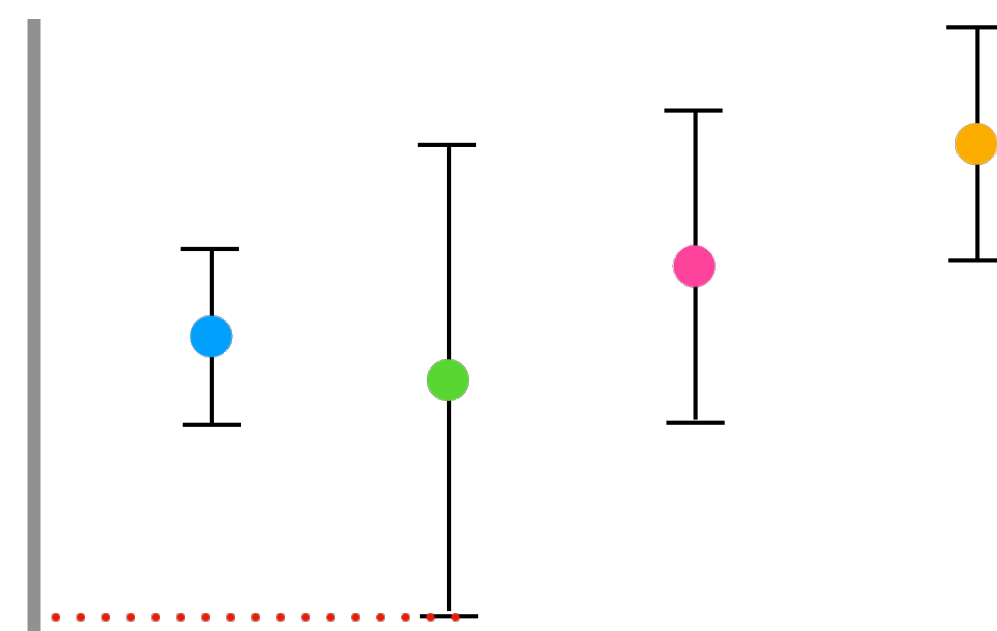
$$H_1 : m(G) \geq c \quad \forall G$$



Maximal c such that $\forall G$:

$$c \leq m(G) + 1.64 \sqrt{\frac{m(G)(1 - m(G))}{n_G}}$$

Interpretation: Model is ‘fair up to c ’—likely performs up to c -well for all groups.



Maximal c such that $\forall G$:

$$c \leq m(G) - 1.64 \sqrt{\frac{m(G)(1 - m(G))}{n_G}}$$

Interpretation: Model is ‘unfair above c ’—model likely does not perform at least c -well for some group at any $c' > c$.

Theoretical Analysis: Meets Desiderata?

Minimal Justice

- Same fairness standard c for all groups
- Fairness as *sufficiency* instead of equality

Incentive Compatibility

- Not susceptible to gaming (no “levelling down”) because fairness defined in terms of *absolute* model performance
- **Pessimistic** metric incentivizes data collection (to reject hypothesis)
- **But optimistic** metric may *discourage* data collection on small groups

Empirical Analysis

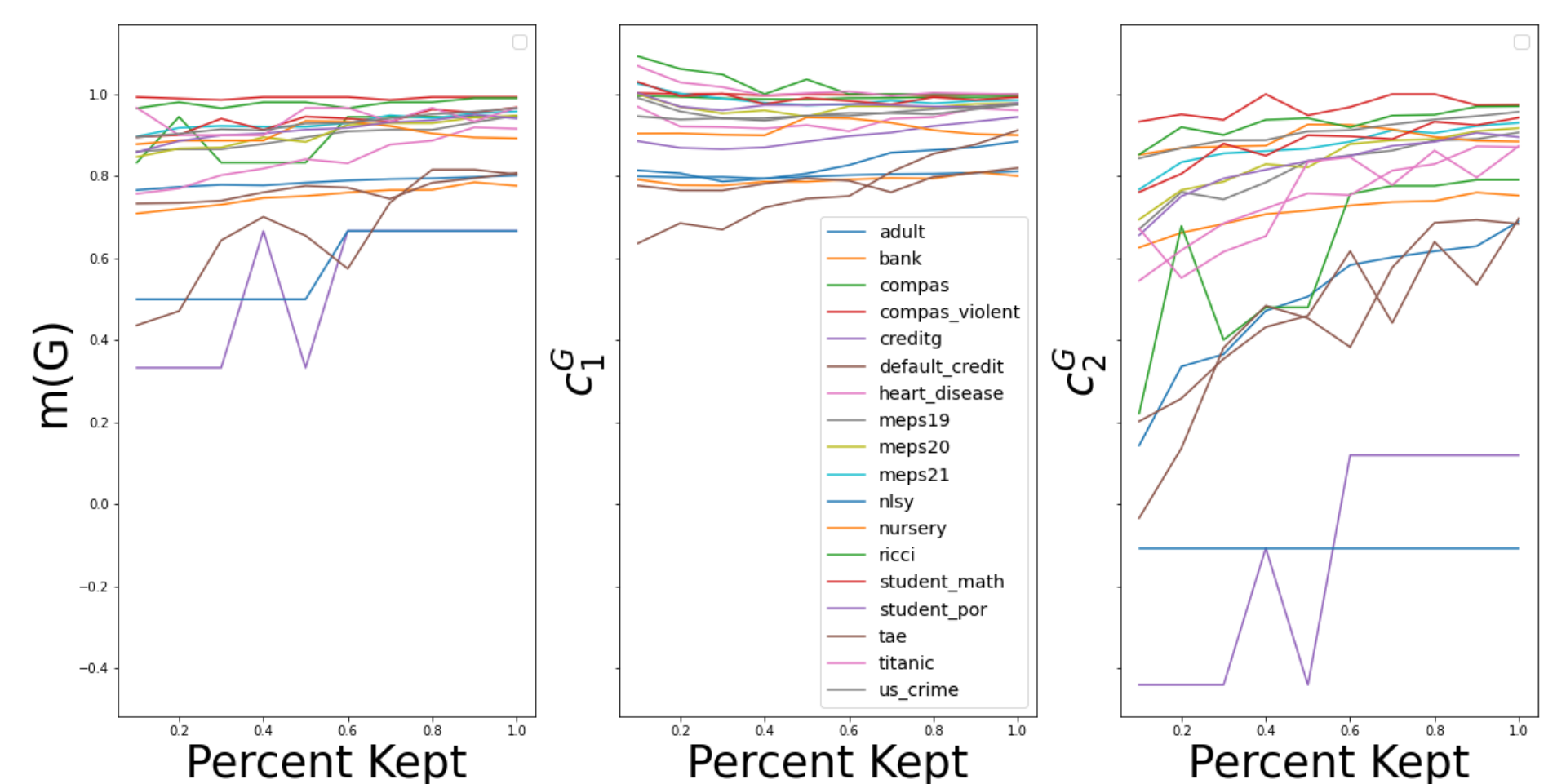
- Test whether proposed metrics meet Incentive Compatibility
- Method
 - **18 fairness datasets** from IBM's lale library
 - XGBoost models with 3-fold cross-validation using lale
 - **Identify critical subgroups:** Minimum accuracy, minimum c_1 , minimum c_2
 - **Subsampling** experiments on critical subgroups and full datasets

Result: Both metrics satisfy Incentive Compatibility

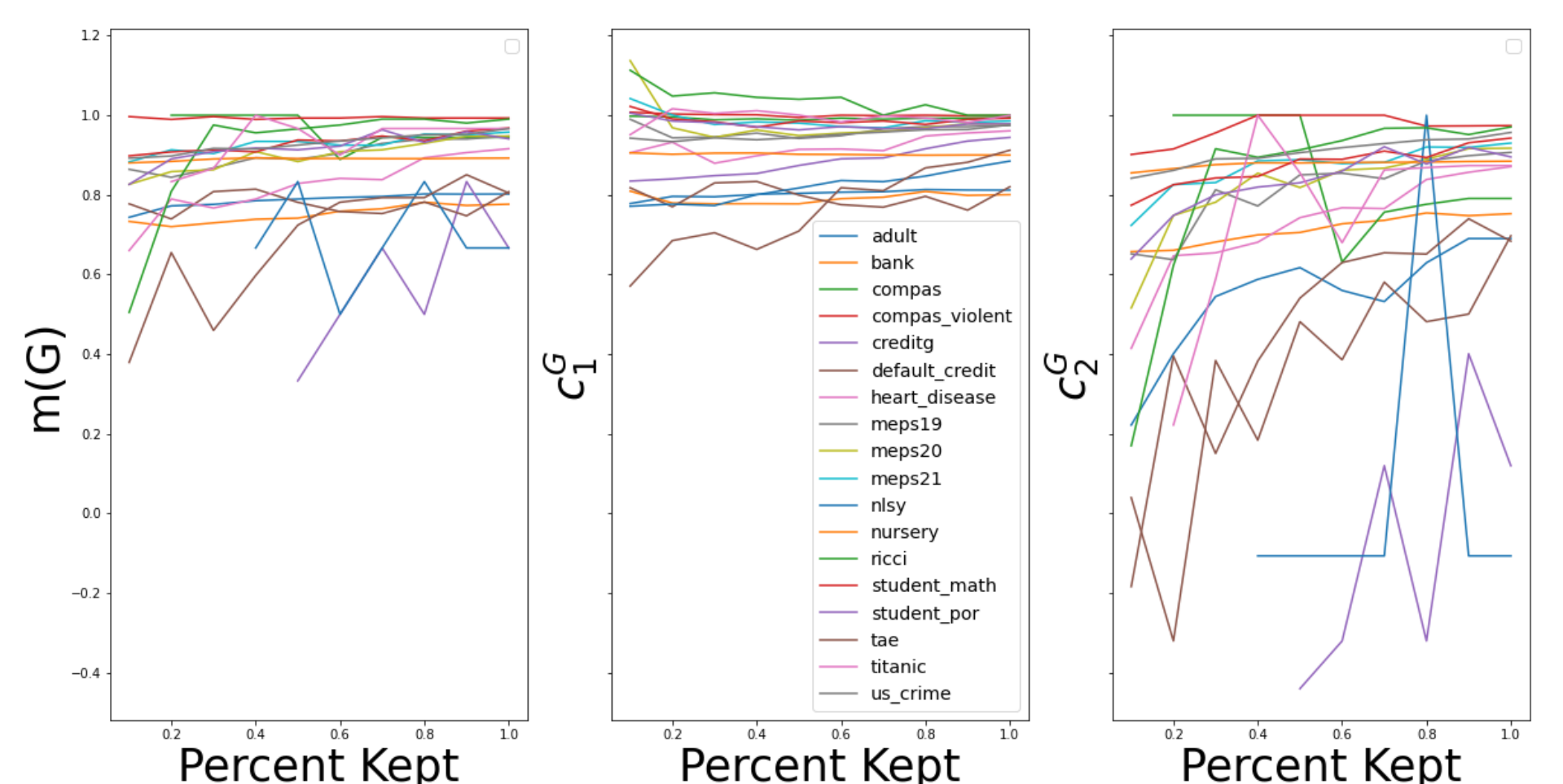
Both the **Optimist's Metric** and **Pessimist's Metric** increase as data increase, indicating they satisfy Incentive Compatibility.

$$m(G) = \text{accuracy, group } G \quad c_1^G = \text{Optimist's} \quad c_2^G = \text{Pessimist's metric}$$

Subsampling only the Critical Subgroup



Subsampling the Entire Dataset



Summary

- Describe intersectionality problem for fairness estimation
- Develop desiderata to guide search for fairness metrics
- Illustrate desiderata with metrics based on hypothesis testing
- **Explore fundamentally different approach:** fairness as *sufficiency* (not equality), accounting for *uncertainty* (not point estimates)
- *Does existing literature sufficiently consider statistical uncertainty in estimating fairness?*

